Q-2) Check the following series for converge:

(i)
$$\sum_{n=2}^{\infty} \frac{3n+7}{(8n^2+11n+2007)(\ln n)^2}$$
 (ii) $\sum_{n=1}^{\infty} \frac{1\cdot 3\cdot 5\cdots (2n+1)}{e^n n!}$

Solution:

(i): Limit compare with $\sum \frac{1}{n(\ln n)^2}$ which converges by the integral test, to conclude that the given series converges.

(ii): Use ratio test, $\frac{a_{n+1}}{a_n} = \frac{2n+3}{e(n+1)} \rightarrow \frac{2}{e} < 1$ as $n \rightarrow \infty$, to conclude that the series converges.