

Due Date: 10 November 2016,
Thursday, Class Time



NAME:.....

STUDENT NO:.....

Math 503 Complex Analysis - Homework 2

1	2	3	4	TOTAL
25	25	25	25	100

Please do not write anything inside the above boxes!

Check that there are **4** questions on your booklet. Write your name on top of every page. Show your work in reasonable detail. A correct answer without proper or too much reasoning may not get any credit.

Submit your solutions on this booklet only. Use extra pages if necessary.

Rules for Homework Assignments

- (1) You may discuss the problems with your classmates or with me but it is absolutely mandatory that you **write your answers alone**.
- (2) You must obey the usual rules of attribution: all sources you use must be explicitly cited in such a manner that the source is easily retrieved with your citation. This includes any ideas you borrowed from your friends. (It is a good thing to borrow ideas from friends but it is a bad thing not to acknowledge their contribution!)
- (3) Even if you find a solution online, you must rewrite it in your own narration, fill in the blanks if any, making sure that you **exhibit your total understanding of the ideas involved**.

Affidavit of compliance with the above rules: I affirm that I have complied with the above rules in preparing this submitted work.

Please sign here:

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Q-1 We know (by Theorem 7.2 on page 97) that for any entire function f and any $R > 0$,

$$\frac{1}{2\pi i} \int_{|z|=R} \frac{f'(z)}{f(z)} dz = \text{The number of zeros of } f, \text{ counting multiplicities, that lie in } |z| < R.$$

Using this theorem give a proof of the Fundamental Theorem of Algebra.

Solution:

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Q-2) Let γ be the polygon $[0, 2, 2 + 2i, 2i, 0]$. Find $\int_{\gamma} f$ for

$$(a) f(z) = \frac{1}{(z - \frac{1}{2} - i)(z - 1 - \frac{3}{2}i)(z - 1 - \frac{i}{2})(z - \frac{3}{2} - i)}.$$

$$(b) f(z) = \frac{1}{(z - \frac{1}{4}[1 + i])(z - \frac{1}{2}[1 + i])(z - \frac{3}{4}[1 + i])}.$$

Solution:

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Q-3 Give an example of a closed rectifiable curve γ such that for any integer k there is a point $a \notin \gamma$ with $n(\gamma; a) = k$.

Solution:

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Q-4) Evaluate the following integral for $n = 1$ and $n = 2$.

$$\int_{|z-\frac{3}{2}|=\frac{3}{2}} \left(\frac{z}{z^2 - 3z + 2} \right)^n dz.$$

Solution: